

# Quantum Physics 1

2015-2016

Lecture of 9 September 2015 and later



# Homework for week 3 of the course

**Study: Chapters 2 and 3,  
emphasis on sections 2.4, 3.1, 3.2, 3.6  
and Eqs. [2.111]-[2.113] (Dirac delta function in Sec. 2.5, )  
(2.1, 2.2, 2.3 was last week)**

See <http://www.quantumdevices.nl/teaching/>

**Problems:**

**To be made before the tutorial session**

**Chapter 2 - 2.18, 2.19, and 2.21**

**Chapter 3 - 3.1, 3.3, and 3.22**

# Previous lectures

## QUANTUM MECHANICS

**The essential differences between classical mechanics and quantum mechanics concerns:**

- 1) The state of a physical system**
- 2) The time evolution of a physical system**
- 3) Making measurements on a physical system**

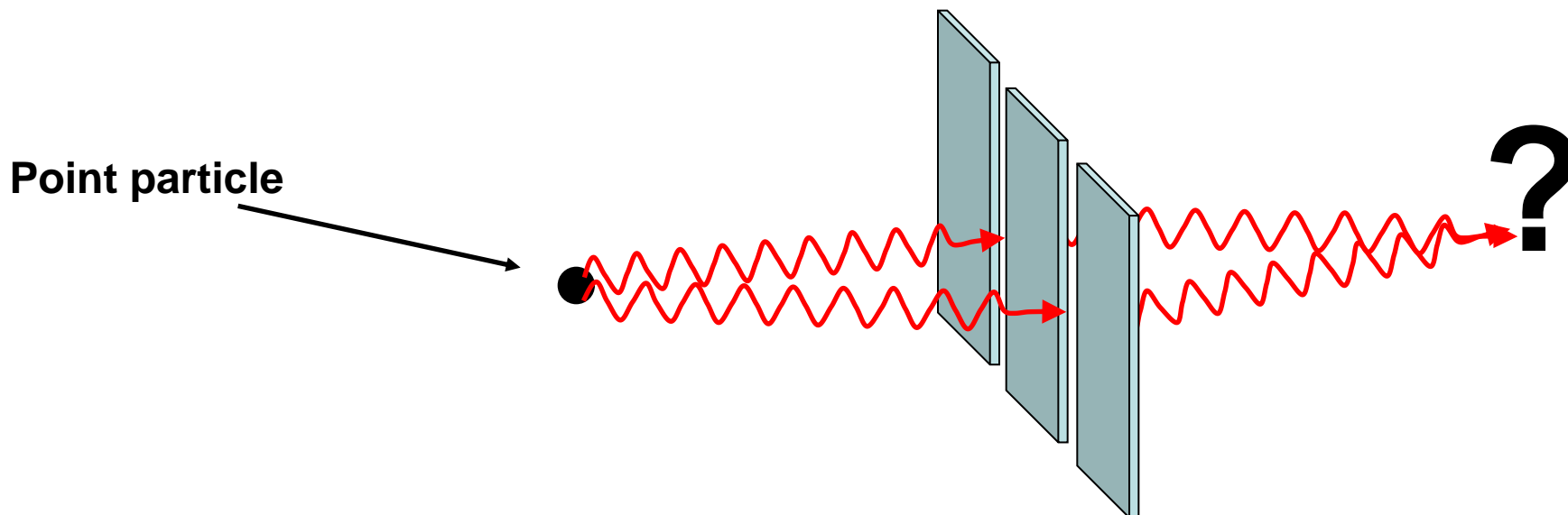
***& this in the form of 5 postulates***

# Today:

## Quantum interference of wave functions

(lecture follows the extra study material from the Feynman Lectures - handout)

### Double slit experiments.



Big hard bullets

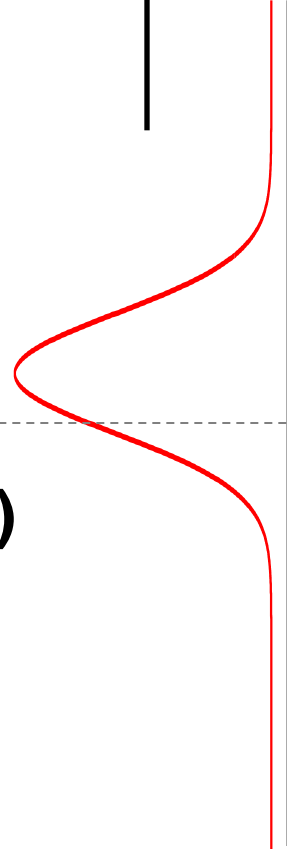
Y-direction



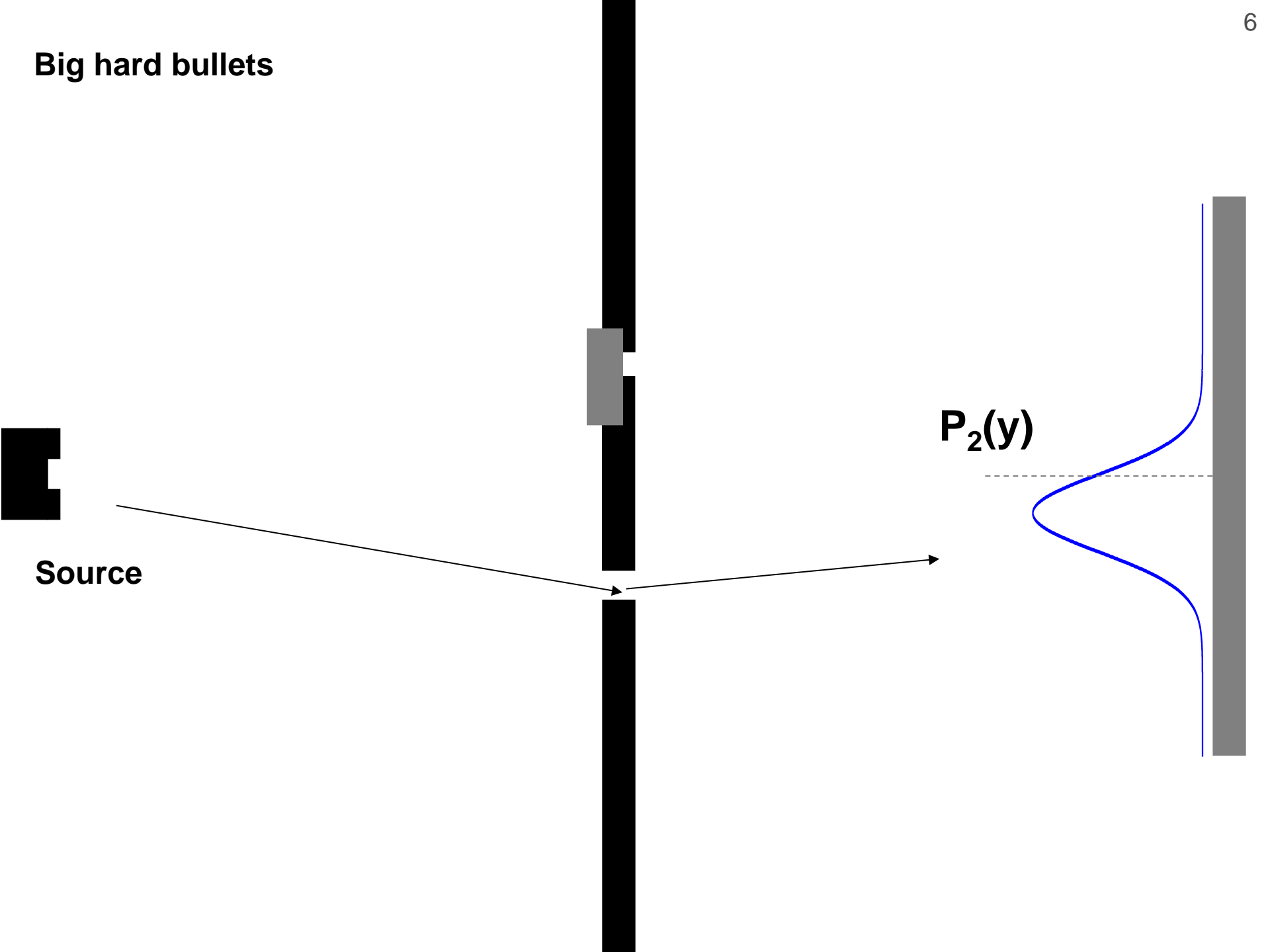
Source  
All bullets have the  
same  $E_{\text{kin}}$



$P_1(y)$



# Big hard bullets



Source

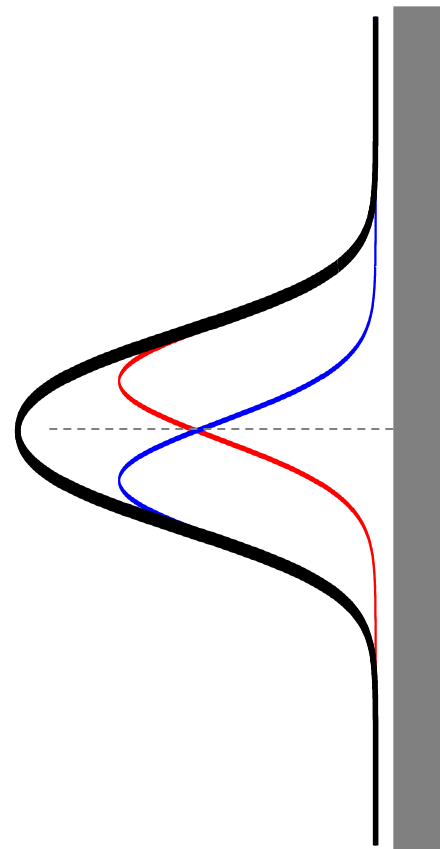
$P_2(y)$

Big hard bullets



Source

$$P_{\text{tot}}(y) = P_1(y) + P_2(y)$$

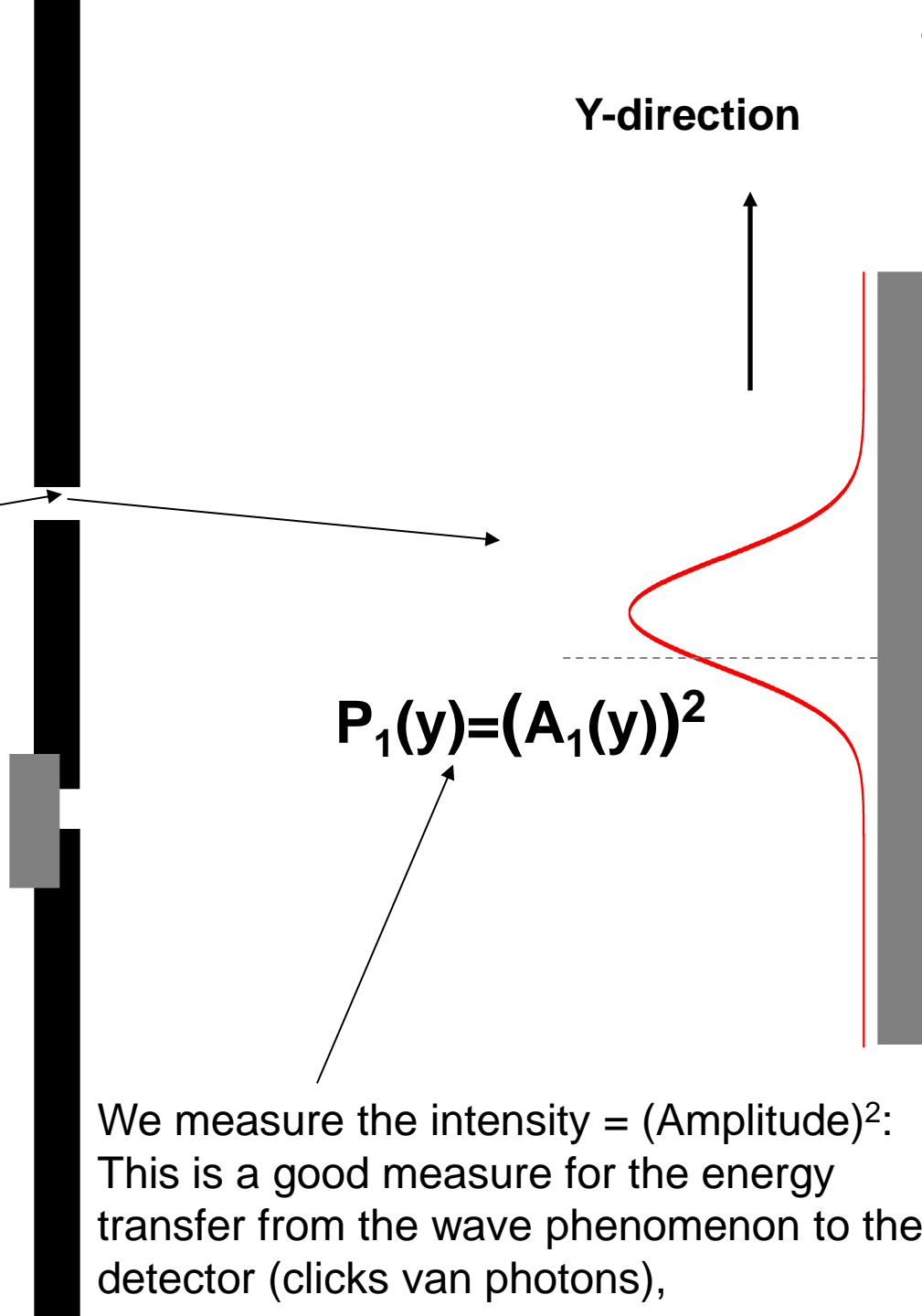


Detection by clicks!

Now a classical wave phenomenon  
For example water waves



Oscillating source,  
monochromatic



We measure the intensity = (Amplitude)<sup>2</sup>:  
This is a good measure for the energy  
transfer from the wave phenomenon to the  
detector (clicks van photons),



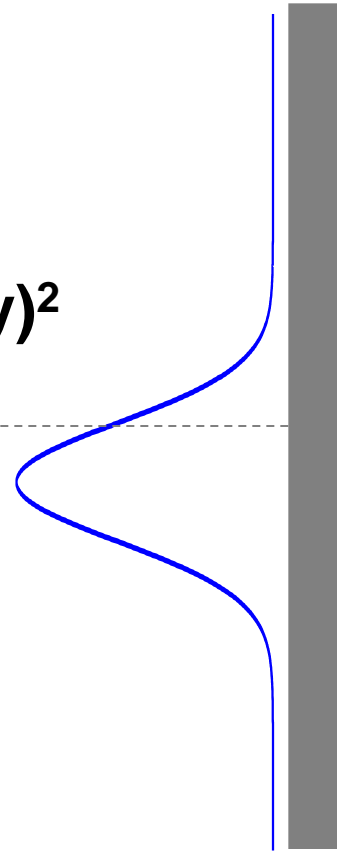
Now a classical wave phenomenon  
For example water waves



Source



$$P_2(y) = A_2(y)^2$$



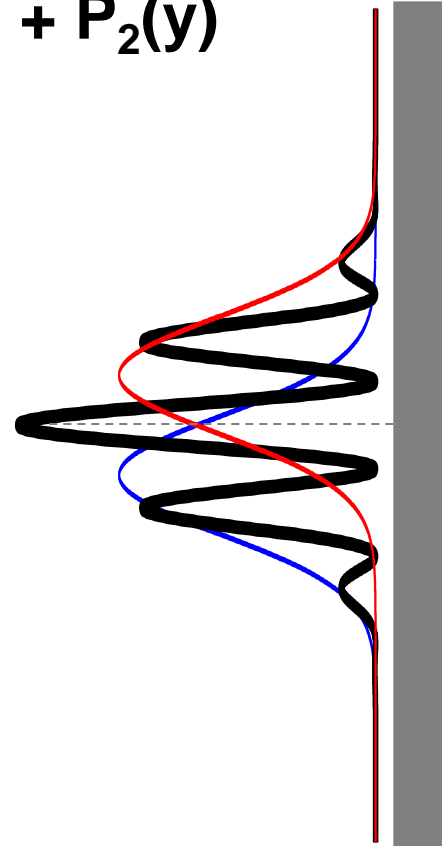
Now a classical wave phenomenon  
For example water waves

$$P_{\text{tot}}(y) = [A_1(y) + A_2(y)]^2$$

not  $P_1(y) + P_2(y)$



Source



Detection of continuously  
changing values!

Now a quantum particle  
For example an electron

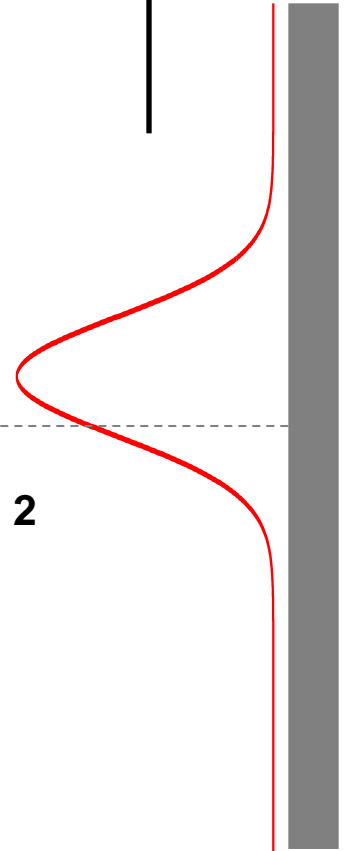


Source  
All electrons have  
the same  $E_{\text{kin}}$



$$P_1(y) = |\Psi_1(y)|^2$$

Y-direction



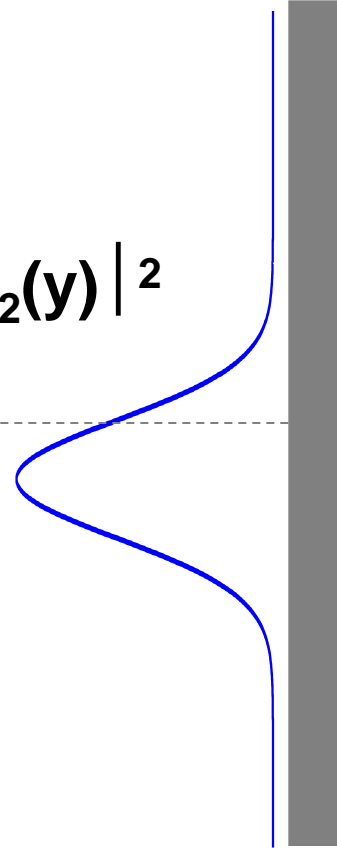
Now a quantum particle  
For example an electron



Source



$$P_2(y) = |\Psi_2(y)|^2$$



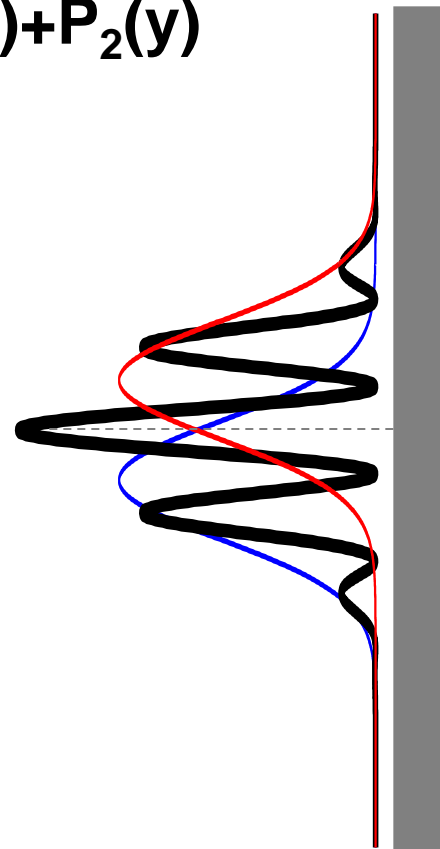
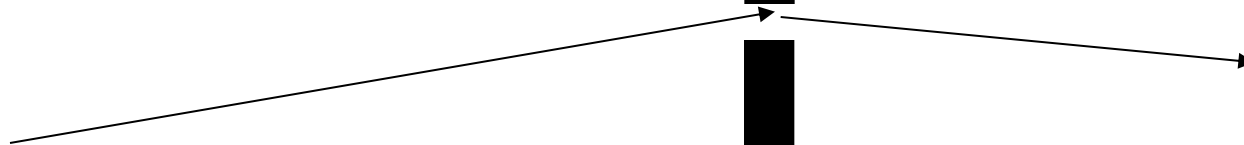
Now a quantum particle  
For example an electron

$$P_{\text{tot}}(y) = |\Psi_1(y) + \Psi_2(y)|^2$$

not  $P_1(y) + P_2(y)$



Source



Detection by clicks!

## Conclusion:

Quantum particles move as a wave, but are detected as a small hard bullet, by clicks that indicate integer chunks, quanta.

How long is the wavelength?

De Broglie

$$\lambda = \frac{h}{p}$$

for photons, electrons,  
....and all moving masses!

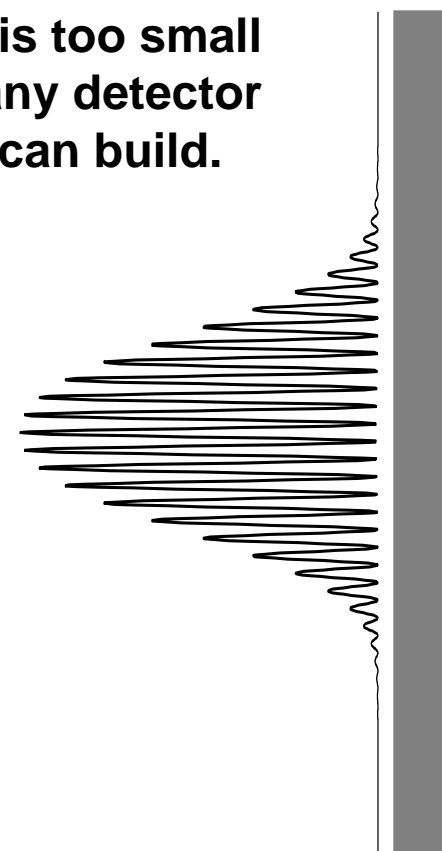
**Big hard bullets**  
- also a quantum particle?

$$\lambda = \frac{h}{p}$$

**p is very large, so the distance between max and min is too small for any detector you can build.**



**Bron**

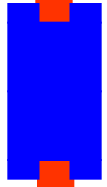
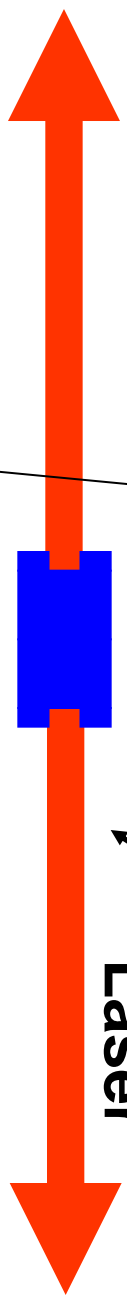


**.....more reasons for the loss of the interference pattern**

Quantum particle –  
Let's look through which slit  
the particle is flying



Source: emission of electrons  
one by one

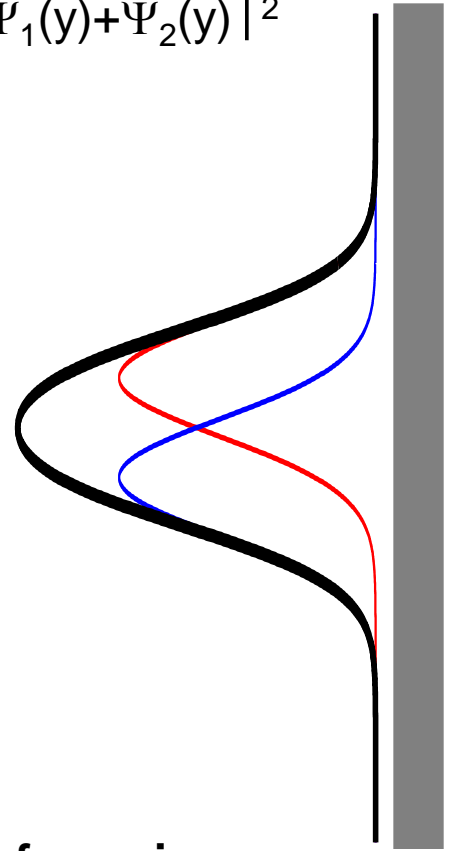


But now, we observe again

$$P_{\text{tot}}(y) = P_1(y) + P_2(y) !$$

and **NO** longer

$$P_{\text{tot}}(y) = |\Psi_1(y) + \Psi_2(y)|^2$$



Detection of passing  
electrons. One always  
observes one full electron at  
only one of the two slits!



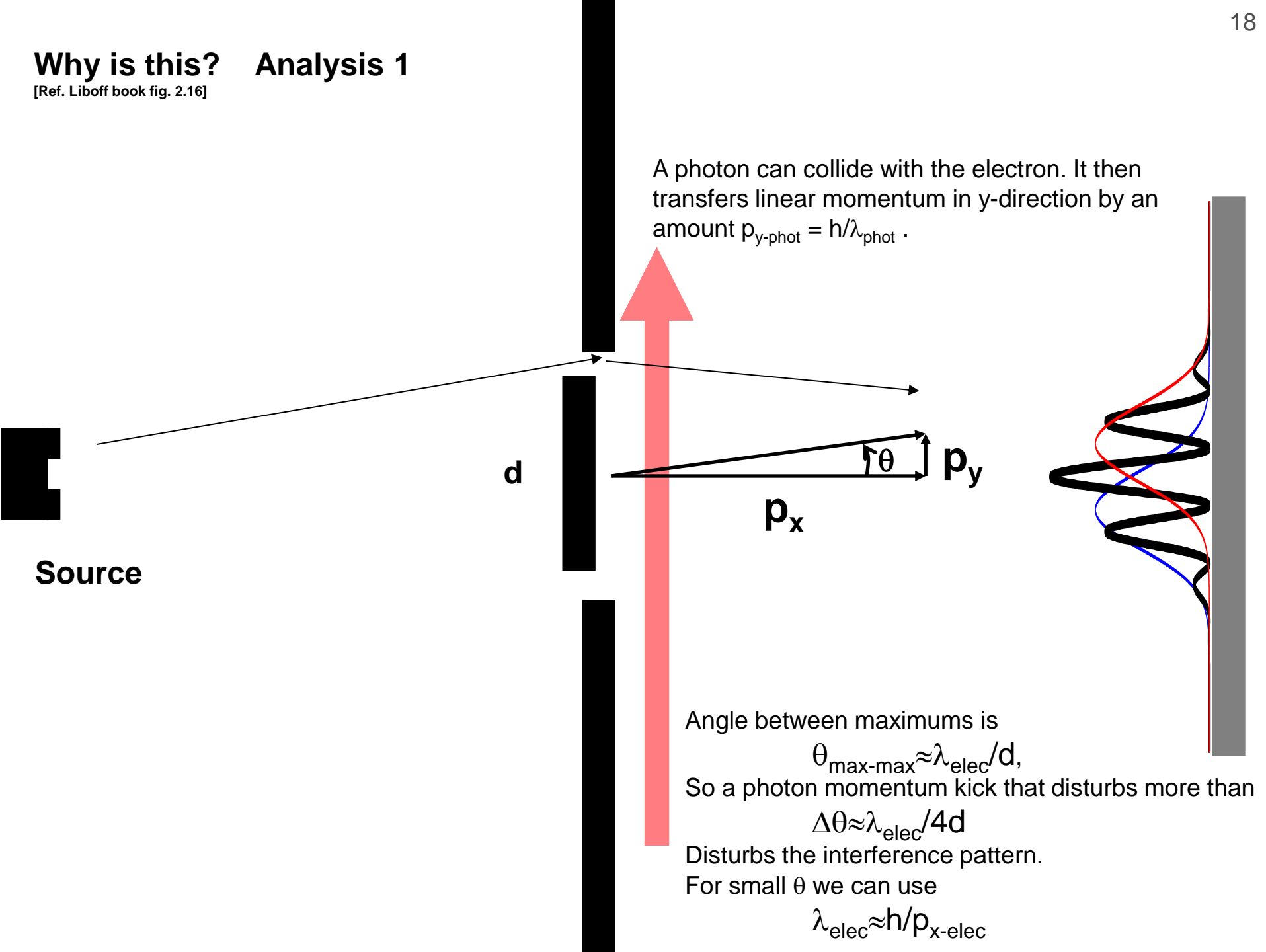
## **Conclusion:**

**Determining through which slit the electron is flying and observing the interference patterns cannot happen at the same time!**

**Why is this?**

# Why is this? Analysis 1

[Ref. Liboff book fig. 2.16]



## Analysis 1 continued

The angle between maximums is

$$\theta_{\text{max-max}} \approx \lambda_{\text{elec}}/d,$$

so a photon momentum kick that disturbs  $\theta$  more than

$$\Delta\theta \approx \lambda_{\text{elec}}/4d$$

disturbs the interference pattern very strongly.

For small  $\theta$  we can use

$$\lambda_{\text{elec}} \approx h/p_{x\text{-elec}}$$

Preventing a  $p_{y\text{-elec}}$  disturbance has as requirement

$$\Delta p_{y\text{-elec}} \approx \Delta\theta p_{x\text{-elec}} < (\lambda_{\text{elec}}/4d) \cdot p_{x\text{-elec}} \approx (h/p_{x\text{-elec}}) \cdot (1/4d) \cdot p_{x\text{-elec}} = h/4d$$

Sufficient resolution for determining the position of the electron requires

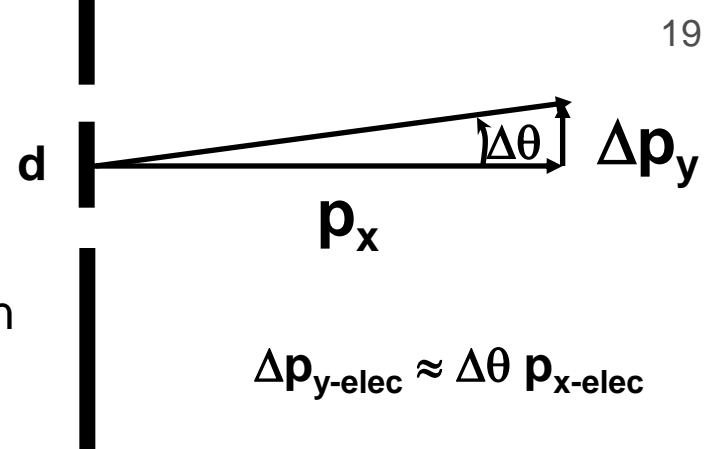
$$\Delta y_{\text{elec}} < d/4.$$

The product of these two requirements together gives

$$\Delta p_{y\text{-elec}} \Delta y_{\text{elec}} \ll (h/4d)(d/4) = h/16.$$

Heisenberg, however, states that this is impossible!

Nature ALWAYS requires that  $\Delta p_{y\text{-elec}} \Delta y_{\text{elec}} > h/2 \approx h/12$



## What is this? – Analysis 2 (Feynman Lectures, handout of this week)

Having sufficient position resolution for determining the position of the electron near the slit requires

$$\Delta y < d/4.$$

This can only be done with a photon that has a wavelength that is not too large,

$$\lambda_{\text{phot}} < d/4.$$

Therefore, the momentum kick of the photon is at least

$$\Delta p_{y\text{-elec}} = h/\lambda_{\text{phot}} > 4h/d.$$

This is more than the  $\Delta p_{y\text{-elec}}$  that gives the limit above which the interference pattern will be disturbed (see previous slide).

# Recent research

**We are still learning quantum physics...**

<http://physics.aps.org/synopsis-for/10.1103/PhysRevLett.109.100404>

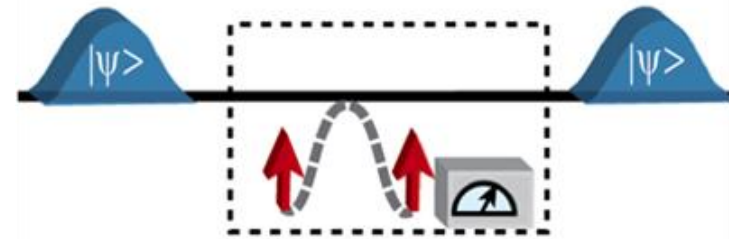
Phys. Rev. Lett. **109**, 100404 (2012)

## The Certainty of Uncertainty

When first taking quantum mechanics courses, students learn about Heisenberg's uncertainty principle, which is often presented as a statement about the intrinsic uncertainty that a quantum system must possess. Yet Heisenberg originally formulated his principle in terms of the "observer effect": a relationship between the precision of a measurement and the disturbance it creates, as when a photon measures an electron's position. Although the former version is rigorously proven, the latter is less general and—as recently shown—mathematically incorrect. In a paper in *Physical Review Letters*, Lee Rozema and colleagues at the University of Toronto, Canada, experimentally demonstrate that a measurement can in fact violate Heisenberg's original precision-disturbance relationship.

If the observer affects the observed, how can one even make such a measurement of the disturbance of a measurement? Rozema *et al.* use a procedure called "weak" quantum measurement: if one can probe a quantum system by means of a vanishingly small interaction, information about the initial state can be squeezed out with little or no disturbance. The authors use this approach to characterize the precision and disturbance of a measurement of the polarizations of entangled photons. By comparing the initial and final states, they find that the disturbance induced by the measurement is less than Heisenberg's precision-disturbance relation would require.

While the measurements by Rozema *et al.* leave untouched Heisenberg's principle regarding inherent quantum uncertainty, they expose the pitfalls of its application to measurements' precision. These results not only provide a demonstration of the degree of precision achievable in weak-measurement techniques, but they also help explore the very foundations of quantum mechanics. — *David Voss*



PRL **109**, 100404 (2012)

PHYSICAL REVIEW LETTERS

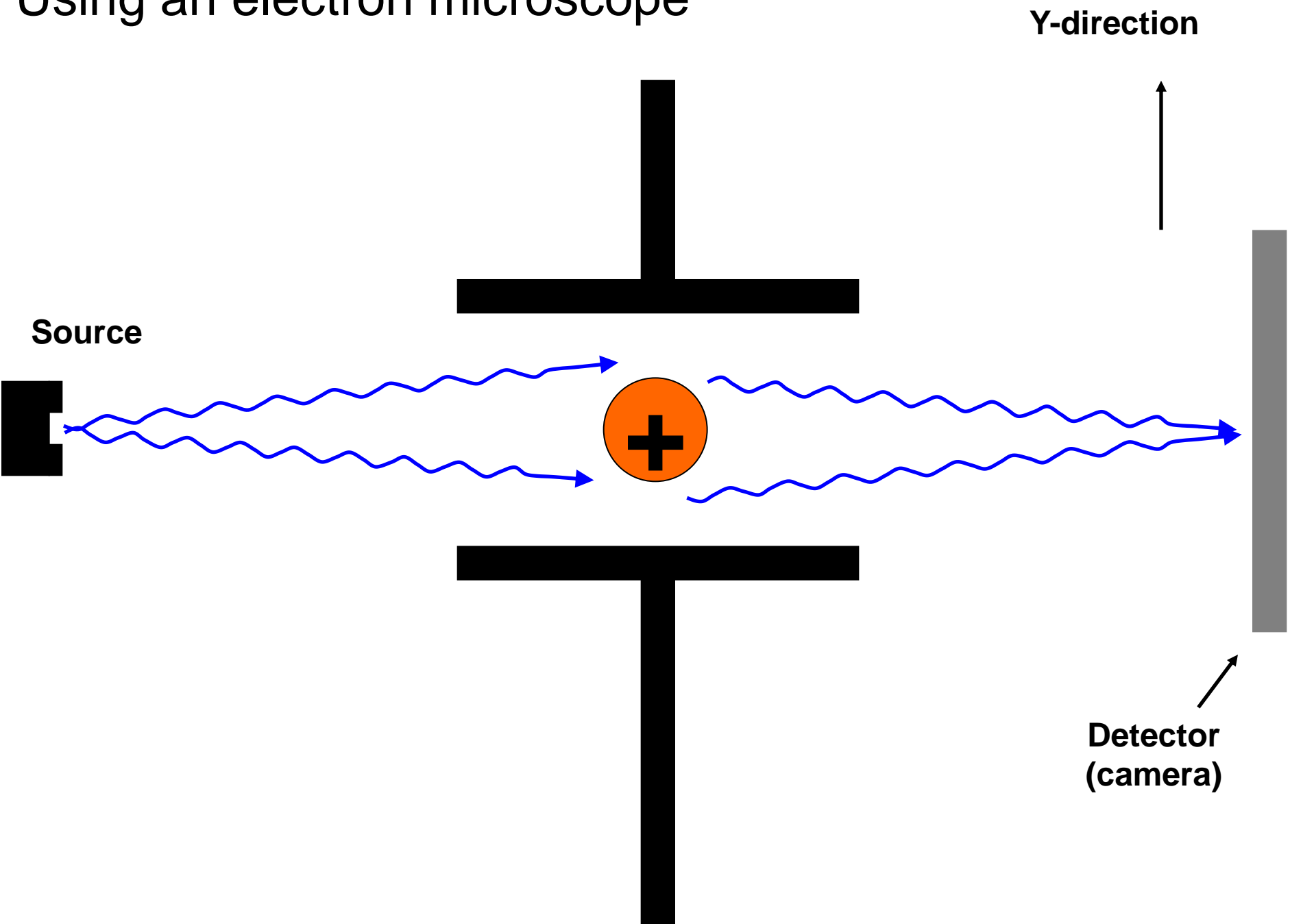
week ending  
7 SEPTEMBER 2012

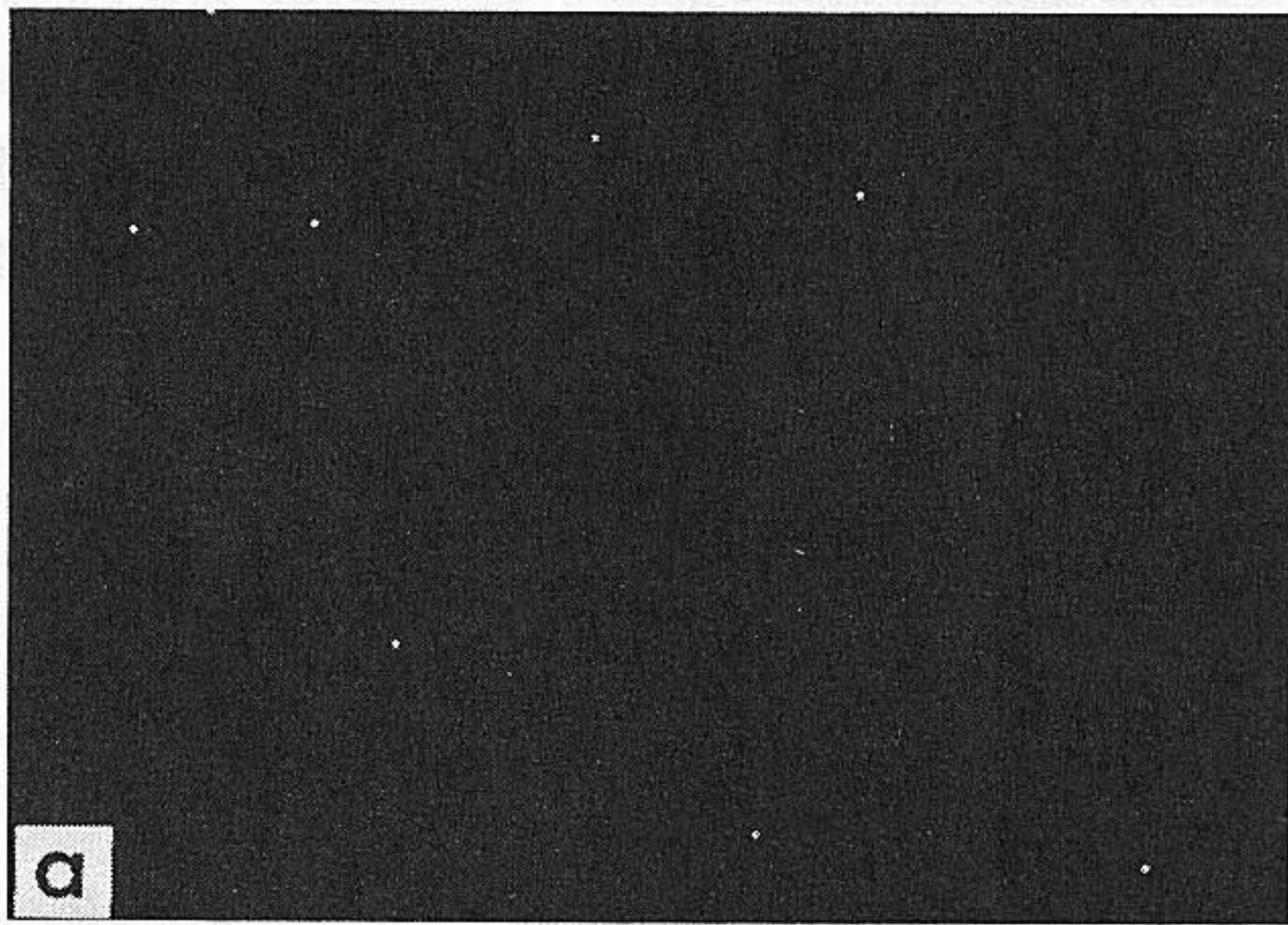


## Violation of Heisenberg's Measurement-Disturbance Relationship by Weak Measurements

Lee A. Rozema, Ardavan Darabi, Dylan H. Mahler, Alex Hayat, Yasaman Soudagar, and Aephraim M. Steinberg

# Using an electron microscope

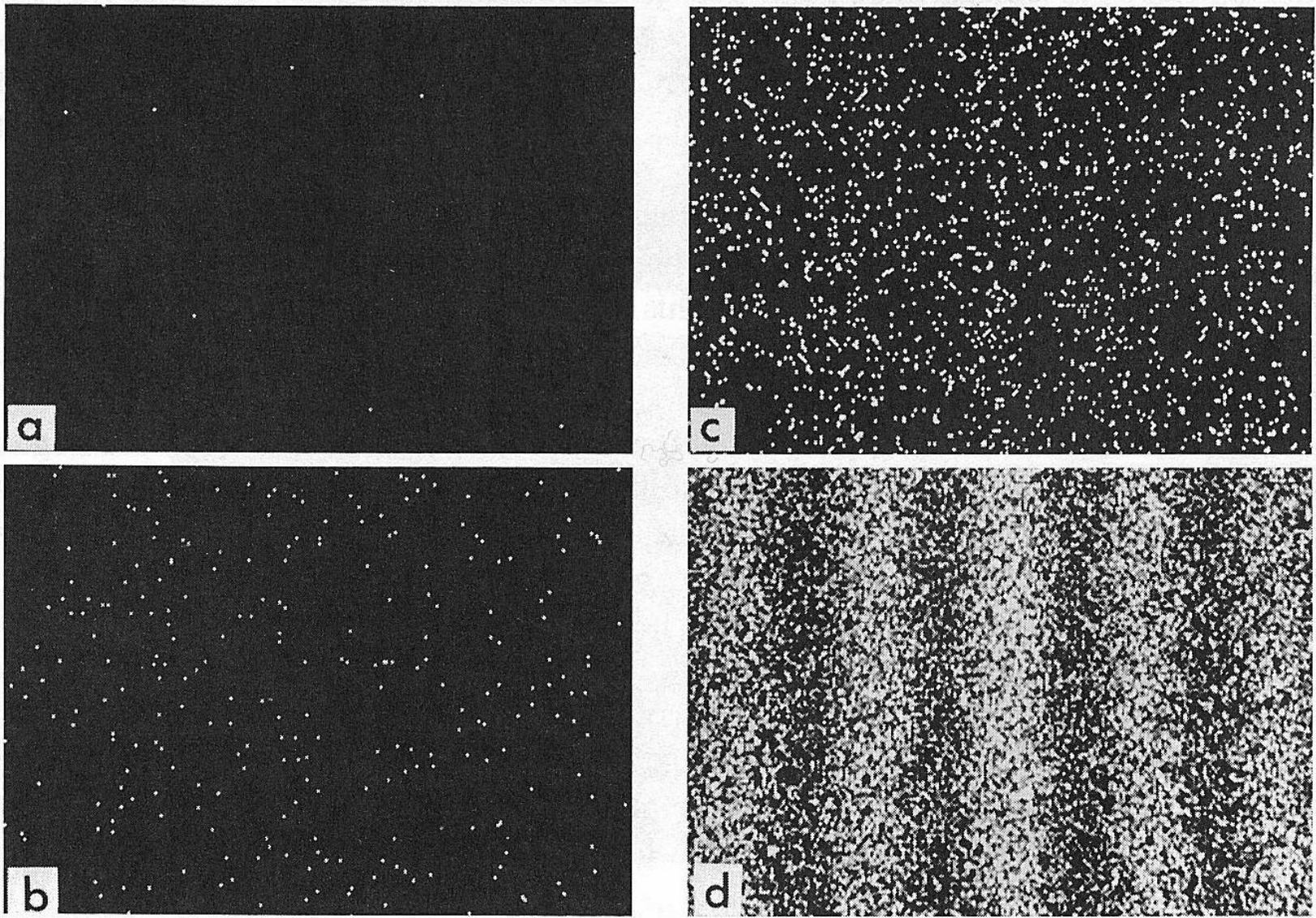




Y-direction  $\longrightarrow$



Source: A. Tonomura, *Annals of the New York Academy of Sciences* 755, p. 227 (1995).



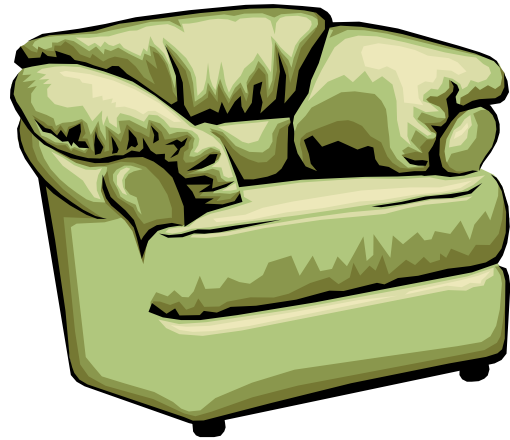
**FIGURE 2.** Single-electron buildup of the electron interference pattern: (a)  $N = 8$ , (b)  $N = 100$ , (c)  $N = 3000$ , and (d)  $N = 100,000$ .

## **Conclusion:**

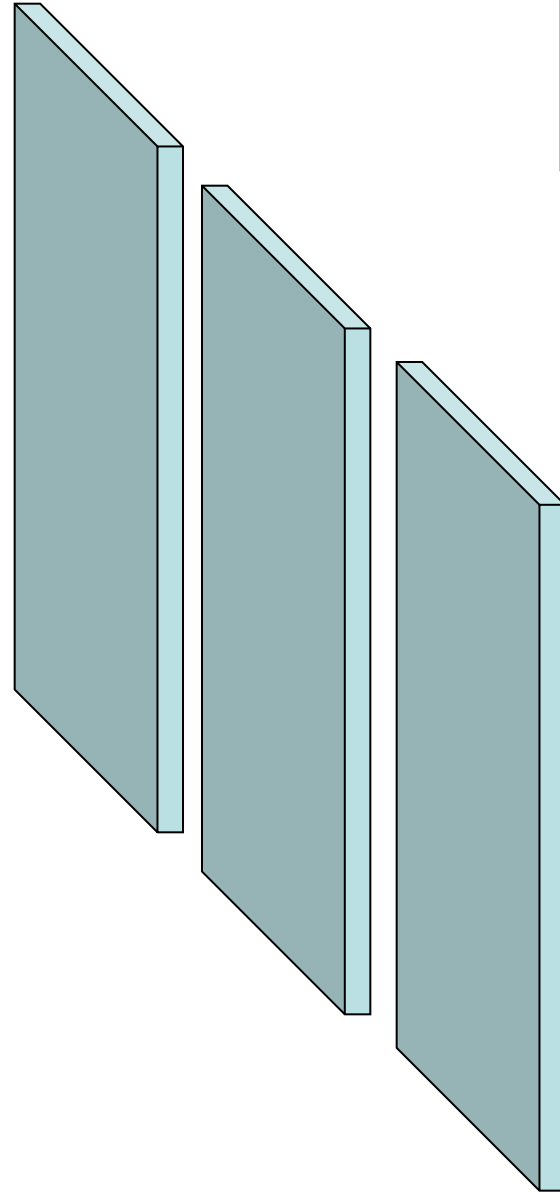
**A quantum particle interferes with itself. For the case here it does not concern interference between the waves of two different particles.**

**When you measure the position of a particle whose y-position is described by a wave function that is a very wide wave front in y-direction, the measurement outcome gives a very specific y-value.**

# Can we show double-slit quantum interference with chairs?



Center of mass motion of the chair



$$\lambda = \frac{h}{p}$$

## Wave Nature of Biomolecules and Fluorofullerenes

Lucia Hackermüller, Stefan Uttenthaler, Klaus Hornberger, Elisabeth Reiger, Björn Brezger,\*  
Anton Zeilinger, and Markus Arndt

*Institut für Experimentalphysik, Universität Wien, Boltzmannngasse 5, A-1090 Wien, Austria<sup>†</sup>*

(Received 7 April 2003; published 28 August 2003)

### letters to nature

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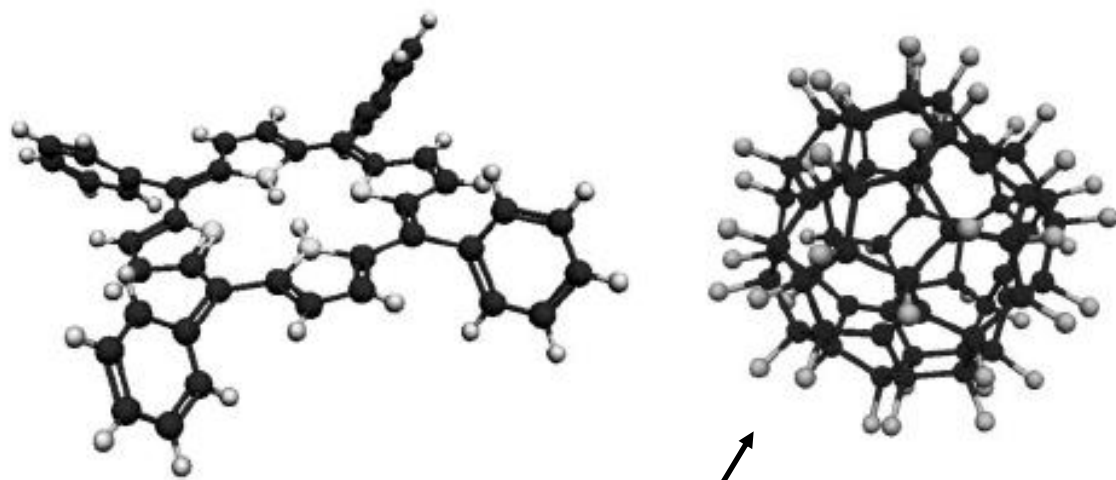
#### Decoherence of matter waves by thermal emission of radiation

Lucia Hackermüller, Klaus Hornberger, Björn Brezger\*,  
Anton Zeilinger & Markus Arndt

<sup>†</sup>*Institut für Experimentalphysik, Universität Wien, Boltzmannngasse 5,  
A-1090 Wien, Austria*

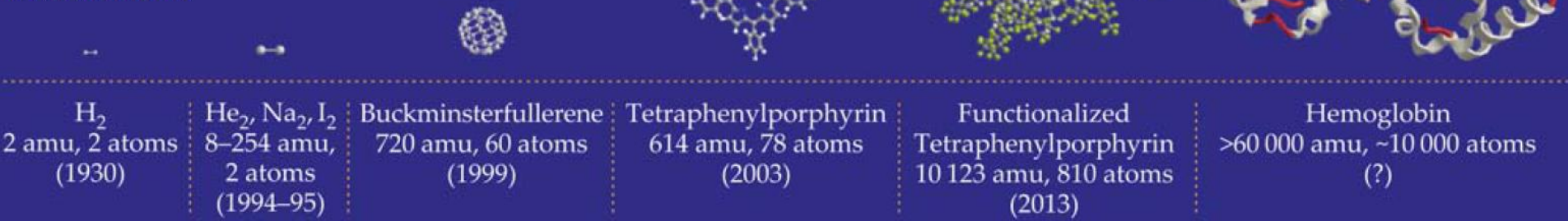
\*Present address: Fachbereich Physik, Universität Konstanz, D-78457 Konstanz, Germany

Nature **427**, 711 (Feb. 2004)



1632 atomic mass units

**Figure 5. Matter-wave diffraction** started in 1930 with diatomic particles, but it didn't gain momentum until the early 1990s. Since then the technique has been extended to progressively larger and more complex molecules; some are depicted here along with their mass in atomic mass units, the number of atoms they comprise, and the year they were first successfully used in interference experiments. To date, a functionalized tetraphenylporphyrin, synthesized by Marcel Mayor and colleagues, is the most massive object for which matter-wave interference has been seen. In the future, bionanomatter such as hemoglobin proteins will likely be studied using matter-wave-enhanced measurements.

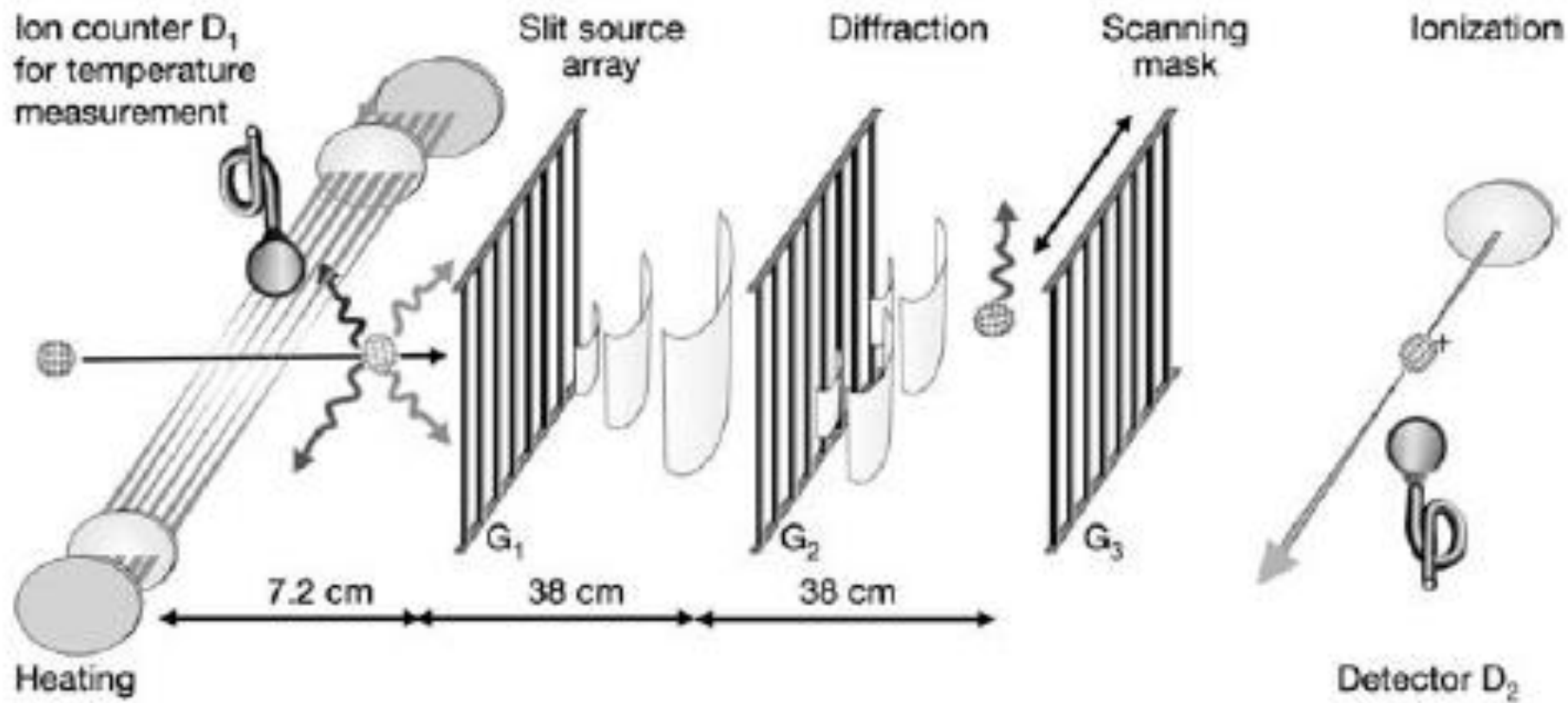


## Reference

(very accessible publication, available on course website):

*Physics Today*, Volume **67**(Issue 5), page 30 (May 2014).





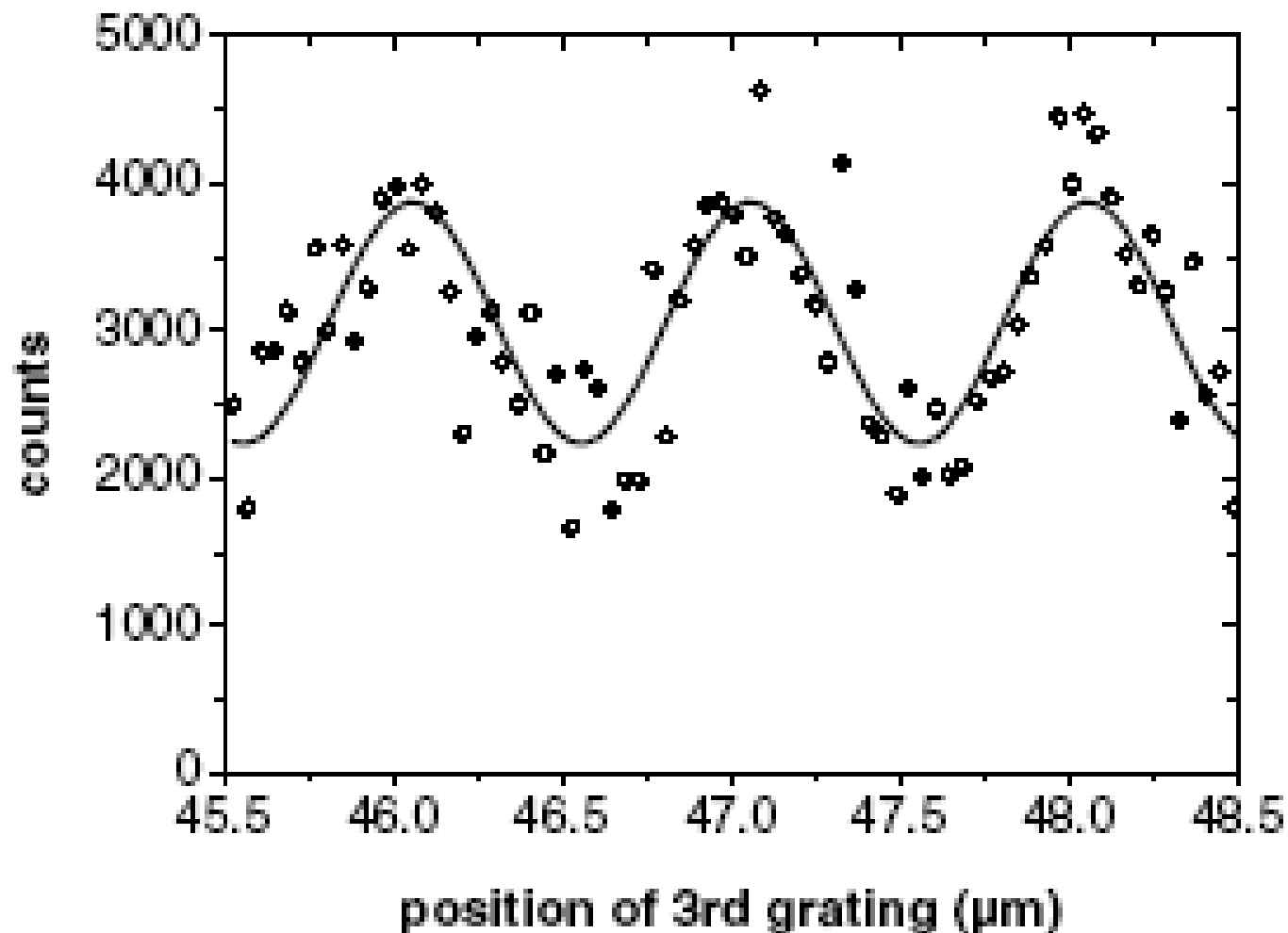
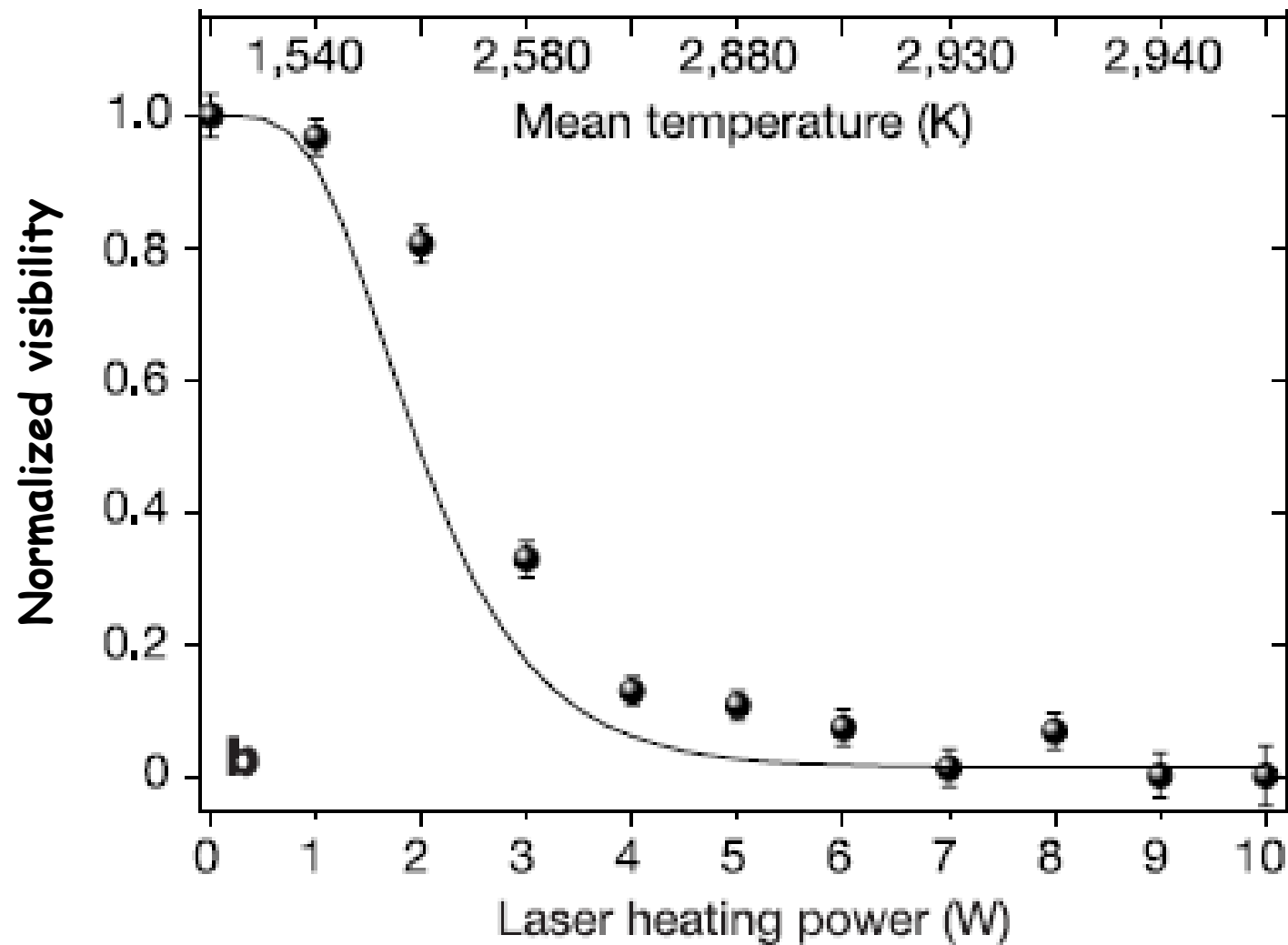


FIG. 4. Quantum interference fringes of  $C_{60}F_{48}$ . The beam has a mean velocity of  $v_m = 105$  m/s and a velocity spread (FWHM) of  $\Delta v/v_m = 20\%$ .





**Why does the interference pattern go away when the temperature of the molecules is made higher?**

**The particle emits black-body radiation, and this can be used for observing along which trajectory the particle is flying:**

**(when  $T$  goes up,  $\lambda$  shorter, position information get more precise).**

**Its is not needed that we (human beings) are around for really making a measurement of this black-body radiation.**

**If there is something in the universe (anything!) that changes in a way that it contains information about which trajectory the particle was taking, the interference pattern will go way.**

# Summary:

1. The positions of both particles and photons are described by a wave function.
2. Such a wave function can interfere with itself.
3. (Lack of) quantum interference is still a topic of hot research.

**Youtube rules: Good summary by Dr. Quantum,  
see <http://www.youtube.com/watch?v=DfPeprQ7oGc>**

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